

Two methods for estimating limits to large-scale wind power generation

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Wind turbines remove kinetic energy from the atmospheric flow, which reduces wind speeds and limits generation rates of large wind farms. These interactions can be approximated using a vertical kinetic energy (VKE) flux method, which predicts that the maximum power generation potential is 26% of the instantaneous downward transport of kinetic energy using the preturbine climatology. We compare the energy flux method to the Weather Research and Forecasting (WRF) regional atmospheric model equipped with a wind turbine parameterization over a 10^5 km² region in the central United States. The WRF simulations yield a maximum generation of $1.1 \text{ W}_e \cdot \text{m}^{-2}$, whereas the VKE method predicts the time series while underestimating the maximum generation rate by about 50%. Because VKE derives the generation limit from the preturbine climatology, potential changes in the vertical kinetic energy flux from the free atmosphere are not considered. Such changes are important at night when WRF estimates are about twice the VKE value because wind turbines interact with the decoupled nocturnal low-level jet in this region. Daytime estimates agree better to 20% because the wind turbines induce comparatively small changes to the downward kinetic energy flux. This combination of downward transport limits and wind speed reductions explains why large-scale wind power generation in windy regions is limited to about $1 \text{ W}_e \cdot \text{m}^{-2}$, with VKE capturing this combination in a comparatively simple way.

generation limits | turbine–atmosphere interactions | wind resource | kinetic energy flux | extraction limits

Wind power has progressed from being a minor source of electricity to a technology that accounted for 3.3% of electricity generation in the United States and 2.9% globally in 2011 (1, 2). Combined with an increase in quantity, the average US wind turbine also changed from 2001 to 2012; hub height increased by 40%, rotor-swept area increased by 180%, and rated capacity increased by 100% (2). Likely a combination of both the above-noted technological innovations and improved siting, the per-turbine capacity factor, the ratio of the electricity generation rate (MW_e) to the rated capacity (MW_i), increased globally from 17% in 2001 to 29% in 2012 (1, 2), making a recently deployed wind farm likely to generate about 70% more electricity from the same installed capacity.

Combining climate datasets with these observed trends of greater-rated capacities and capacity factors, several academic and government research studies estimate large-scale wind power electricity generation rates of up to $7 \text{ W}_e \cdot \text{m}^{-2}$ (3–7). However, a growing body of research suggests that as larger wind farms cover more of the Earth's surface, the limits of atmospheric kinetic energy generation, downward transport, and extraction by wind turbines limits large-scale electricity generation rates in windy regions to about $1.0 \text{ W}_e \cdot \text{m}^{-2}$ (8–14). Ideally, these inherent atmospheric limitations to generating electricity with wind power could be considered without scenario- and technology-specific complex modeling approaches, be easily applied to “preturbine” climatologies, and yield spatially and

temporally variable generation rates comparable to the energetically consistent atmospheric modeling methods.

Here, we describe such a simple method that focuses on the vertical downward transport of kinetic energy from higher regions of the atmosphere to the surface. In the absence of wind farms, the downward flux of kinetic energy is dissipated by turbulence near the surface, which shapes near-surface wind speeds. When wind farms use some of this kinetic energy, the vertical balance between the downward kinetic energy flux and turbulent dissipation is altered and results in lower hub-height wind speeds. The more kinetic energy wind farms use, the greater the shift in the balance and the reduction of wind speeds should be. This trade-off between greater utilization and lower wind speeds results in a maximum in wind power generation from the vertical flux of kinetic energy (10). This maximum yields a potential for wind power generation of a region that is independent of the technological specifications of the turbines. Because this method is based on the vertical downward transport of kinetic energy, we refer to it as the vertical kinetic energy (VKE) method. Note that this reasoning assumes that the downward flux of kinetic energy remains unchanged, which was shown to be a reasonable assumption compared with climate model simulations at the continental scale (11), but which may not hold at the regional scale.

Here we evaluate the applicability of this method by using high-resolution simulations with the Weather Research and Forecasting (WRF) regional atmospheric model with a wind turbine parameterization. We use the region of central Kansas during the typical climatological period of June–September 2001, noting that this

Significance

Wind turbines generate electricity by removing kinetic energy from the atmosphere. We show that the limited replenishment of kinetic energy from aloft limits wind power generation rates at scales sufficiently large that horizontal fluxes of kinetic energy can be ignored. We evaluate these factors with regional atmospheric model simulations and find that generation limits can be estimated from the “preturbine” climatology by comparatively simple means, working best when the atmosphere between the surface and hub height is naturally well-mixed during the day. Our results show that the reduction of wind speeds and limited downward fluxes determine the limits in large-scale wind power generation to less than $1 \text{ W}_e \cdot \text{m}^{-2}$.

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period is before large-scale wind power deployment within this region. We then use the WRF simulation of this time period without wind farm effects to obtain the downward transport of kinetic energy into the region. This flux is used by the VKE method to predict the limit for wind power generation of the region. This limit as well as its temporal variations are then compared with a set of sensitivity simulations of the WRF model using different installed capacities of $0.3\text{--}100\text{ MW}_i\text{-km}^{-2}$ to derive the maximum wind power generation rate (the WRF method). These regional results will then be used within a broader interpretation on the role of horizontal and vertical kinetic energy fluxes to wind farms of differing installed capacities and spatial scales. We close with a brief conclusion on the implications of these two approaches for estimating large-scale wind power generation.

Methods

To evaluate the limits to wind power generation, we use a reference climatology of Central Kansas for the time period of May 15 to September 30, 2001 using the WRF-ARW v3.3.1 regional weather forecasting model (15, 16), forced with North American Regional Reanalysis data (17). This particular time period is climatologically representative for this region: a near-neutral El Niño southern oscillation phase, a climatologically standard position and strength of the Great Plains low-level jet, and an average summer soil moisture content (18). The simulation uses a single domain with a horizontal grid spacing of 12 km and 31 vertical levels, and the first 15 d of the simulation are excluded from the analysis to avoid spin-up effects. This WRF simulation represents our control simulation, which is used as input to the VKE method and as a reference for various WRF simulations with different densities of installed wind turbines to obtain the limit for wind power generation using the WRF method.

WRF Method. To estimate wind power generation using WRF, we use a version of the model that includes a parameterization of wind turbines that is slightly modified from a previously used approach (12, 19). This parameterization has been shown to be more realistic than previous roughness-based approaches (19). We perform a set of eight sensitivity simulations with different installed capacities of wind turbines that are placed within a contiguous wind farm region of 112,320 km² in central Kansas. Installed capacities (in units of MW·km⁻²) are simulated as an increased integrated quantity of wind turbines deployed to 780 grid cells of 144 km² each, which collectively represents the wind farm region. We use values of 0.3125, 0.625, 1.25, 2.5, 5.0, 10, 25, and 100 MW·km⁻² for the installed capacities in the simulations and refer to the simulations by these capacities. The wind turbine characteristics are specified using the technical specifications of the Vestas V112 3.0 MW_i in terms of its power, thrust, and standing coefficients (see [SI Appendix](#) for the detailed model configuration). Note that this model setup does not have sufficient horizontal or vertical resolution to simulate interturbine interactions or wakes within the 12- × 12-km resolution grid cell, but rather uses the turbine specifications and installed capacity to derive one aggregate wind turbine for each grid cell and, where appropriate, the corresponding vertical levels. Additional simulations were performed to evaluate the sensitivity to the horizontal (to 3 km) and vertical spacing (to 24 levels in the lowest 1 km, 6 within the vertical rotor swept height) over a representative time period of June 15–21 and were found to yield comparable results ([SI Appendix, Fig. 5](#)).

VKE Flux Method. The VKE method expands upon one of the approaches of refs. 10 and 11, where a thought experiment illustrated how considering only wind speeds and turbine specifications can yield generation rates that are physically unrealizable. The method is based on an analytical description of the momentum balance of the wind farm, a central concept used in similar studies on large-scale wind power limits (20–22) or for other forms of renewable energy such as tidal power (23, 24) (detailed methodology is given in [SI Appendix](#)). It assumes that when wind farms extend tens of kilometers downwind, horizontal kinetic energy has either been extracted from the mean flow by the first few rows of turbines or has been lost to turbulent dissipation, so that the generation rate of wind turbines further downwind is then limited by the downward flux of kinetic energy. For this reason, it is assumed that the horizontal kinetic energy flux can be neglected for large-scale wind farms, allowing us to estimate the maximum extraction rate of kinetic energy by the turbines from the vertical downward flux of kinetic energy from the atmosphere above the wind farm. The model yields an analytic expression for the maximum extraction rate, $P_{\max} = (2\sqrt{3}/9) \cdot \rho u_z^2 \cdot v_0$, where ρ is

the air density, u_* is the friction velocity at the surface, and v_0 is the wind speed of the control simulation at the 84-m hub height. Note that in addition to the wind speed (v_0), this method uses the surface friction velocity (u_*) as an additional meteorological variable to yield the rate P_{max} . This additional information is not used in common methods that evaluate limits to wind power generation using only wind speeds and a prescribed installed capacity (3–7). We then convert this maximum rate into a limit for electricity generation by using the Betz limit and estimates of wake turbulence (25), resulting in a reduction to about 66%, or two-thirds, of P_{max} . Thus, we define the maximum electricity generation rate by a large wind farm as $P_e = (4\sqrt{3}/27) \cdot \rho \cdot u_*^2 \cdot v_0$. This results in the maximum electricity generation rate, P_e , to be equivalent to $(4\sqrt{3}/27) = 26\%$ of the turbulent dissipation occurring before wind farm deployment. Note that P_e is not specific to an installed capacity or wind turbine manufacturer specifications, thereby resulting in the maximum wind power generation rate possible from the pre-turbine climatological vertical kinetic energy flux through hub height.

Results and Discussion

As shown in Fig. 1, the WRF simulations show that a greater installed capacity within the wind farm region increases the total electricity generation rate. This increase is almost linear at the lower installed capacities ($0.3 \text{ MW}_i \cdot \text{km}^{-2} \approx 0.13 \text{ W}_e \cdot \text{m}^{-2}$, $0.6 \text{ MW}_i \cdot \text{km}^{-2} \approx 0.24 \text{ W}_e \cdot \text{m}^{-2}$; subscripts i and e refer to the installed capacity and electricity generation, respectively). With further increases in the installed capacity, the marginal return of electricity generation predominantly occurs during higher wind speed periods. Such greater generation rates during windy periods can be seen in the differences between the simulations with 5.0 and 10 $\text{MW}_i \cdot \text{km}^{-2}$ during the high wind speeds of June, whereas the difference is smaller during the lower wind speeds of August and September. Because the greater generation rates occur during periods that are less frequent, the increase in generation is no longer linear. This is reflected by comparing the generated electricity of the 5.0 $\text{MW}_i \cdot \text{km}^{-2}$ to the 0.3 $\text{MW}_i \cdot \text{km}^{-2}$ simulation, which generates seven times more electricity with 16 times as many wind turbines. Stated differently, each wind turbine at 5.0 $\text{MW}_i \cdot \text{km}^{-2}$ generates electricity at half the rate as wind turbines with the same technical specifications but installed at 0.3 $\text{MW}_i \cdot \text{km}^{-2}$.

This difference in the relationship between generation rate and installed capacity is reflected in a change in the capacity factor. First, we use the hub-height wind speeds of the control simulation and the turbine power curve for the Vestas V112 turbine (*SI Appendix, Fig. 6*) to calculate the generation rate of a single isolated wind turbine deployed to each location and time. This yields a capacity factor of 47%, which represents the upper bound value for the case of no interactions between the wind turbines and the atmospheric flow. This estimate compares well to the capacity factors of 22–36% (1, 7) derived from installed capacity and operational generation data from Kansas during 2006–2012, even though this estimate includes turbines of various technical specifications taken over a much longer timescale than this study. Using the 2012 installed capacity of 2,713 MW_i (7) and the area of 213,000 km² for Kansas yields a state-scale installed capacity of

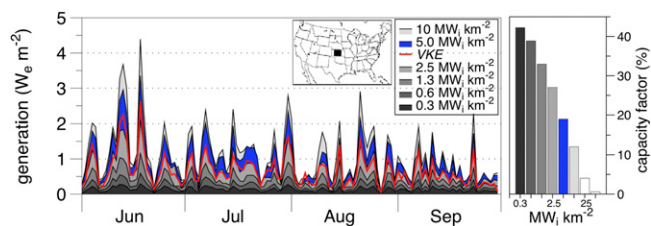


Fig. 1. (Left) Simulated daily mean electricity generation rates over the Kansas wind farm region (black square on map) for different installed capacities of up to 10 MW_t·km⁻². The higher installed capacities of 25 and 100 MW_t·km⁻² are not shown, because they often yield less than the 10 MW_t·km⁻² simulation. For comparison, the VKE estimate is shown in red. (Right) The mean per-turbine capacity factor derived for the different simulations.

$0.013 \text{ MW}_i \cdot \text{km}^{-2}$, which falls below the lowest installed capacity that we used. Our simulation with the lowest installed capacity of $0.3 \text{ MW}_i \cdot \text{km}^{-2}$ corresponds to a slightly reduced capacity factor of 42%, and 39% with $0.6 \text{ MW}_i \cdot \text{km}^{-2}$ (SI Appendix, Table 2). These capacity factors compare well with the previously used values for this region of 37% (6) and 40–47% used by the National Renewable Energy Laboratory (7). However, the estimates of refs. 6 and 7 used an installed capacity of $5.0 \text{ MW}_i \cdot \text{km}^{-2}$, which in our simulations yield a much lower capacity factor of 19%, which should thus result in much lower estimates for wind power generation.

The reduction in capacity factor with greater installed capacity results from an enhanced interaction of wind turbines with the atmospheric flow. Because a greater installed capacity of wind turbines removes more kinetic energy from the atmosphere and converts it into electric energy, this causes a decrease in the hub-height wind speed downwind (26), which decreases the mean per-turbine electricity generation rate of the wind farm. This reduction in wind speeds within the wind farm and its effects on the per-turbine electricity generation rate is shown in Fig. 2 in relation to the power curve of the turbine and the wind speed histogram (Fig. 2A) as well as the mean wind speed and mean per-turbine generation rate (Fig. 2B). The point spread around the 3.0 MW_i turbine power curve in Fig. 2A, with some values below the $3.0 \text{ m} \cdot \text{s}^{-1}$ cut-in wind speed, is due to the use of mean hourly hub-height wind speed and electricity generation rate for the entire wind farm region. Additionally, the variability in hub-height wind speed decreases with greater installed capacity (Fig. 2B), which also decreases the variability of per-turbine electricity generation. This reduction in wind speeds has also been observed in previous modeling studies (9–12, 27, 28).

Fig. 2C shows the increasing importance of considering the reduction in wind speed for the mean generation rate of the wind farm with greater installed capacity. The dashed line in Fig. 2C is derived by applying the turbine power curve to the control hub-height wind speeds for a mean per-turbine capacity factor of 47% (slope = 0.47). The WRF simulations with installed capacities of less than about $1 \text{ MW}_i \cdot \text{km}^{-2}$ yield similar estimates because the capacity factors remain high (see also SI Appendix, Table 2). At greater installed capacities, the WRF simulations resulted in proportionally lower estimates. For example, at an installed capacity of $2.5 \text{ MW}_i \cdot \text{km}^{-2}$ the “no interactions” estimate would yield a generation rate per unit area of the wind farm of $1.18 \text{ W}_e \cdot \text{m}^{-2}$, but this was simulated to be $0.68 \text{ W}_e \cdot \text{m}^{-2}$. This discrepancy continues with greater installed capacities, so at $5.0 \text{ MW}_i \cdot \text{km}^{-2}$ the estimate without interactions overestimates the average electricity generation rate by more than a factor of two ($2.4 \text{ W}_e \cdot \text{m}^{-2}$ for no interactions, $0.95 \text{ W}_e \cdot \text{m}^{-2}$ with interactions). The maximum electricity generation rate of $1.1 \text{ W}_e \cdot \text{m}^{-2}$ is obtained with an installed capacity of $10 \text{ MW}_i \cdot \text{km}^{-2}$, at which the associated hub-height wind speed decreased by 42% and the capacity factor is reduced to 12%. Our WRF simulations suggest that previous estimates of mean wind energy generation potentials for Kansas of $1.9 \text{ W}_e \cdot \text{m}^{-2}$ (6), 2.0 – $2.4 \text{ W}_e \cdot \text{m}^{-2}$ (7), and $2.5 \text{ W}_e \cdot \text{m}^{-2}$ (4) are likely to be too high because the effects of reduced wind speeds were not considered. To place this reduction into the context of present-day wind power deployment, note that such installed capacities are several orders of magnitude larger than presently operational Kansas wind farms. Our simulations thus suggest that an equidistant deployment of 50 times more installed wind power in Kansas than is presently operational (≈ 0.013 – $0.6 \text{ MW}_i \cdot \text{km}^{-2}$) would maintain the presently high per-turbine capacity factors and thus increase the generation rate 50-fold.

The VKE method captures the magnitude of wind power generation as well as its temporal variations. In our Kansas scenario, we estimate a maximum 4-mo mean generation rate from WRF at $10 \text{ MW}_i \cdot \text{km}^{-2}$ as $1.1 \text{ W}_e \cdot \text{m}^{-2}$ and VKE as $0.64 \text{ W}_e \cdot \text{m}^{-2}$. Based on the linear correlation, the daily mean estimates of the two methods are

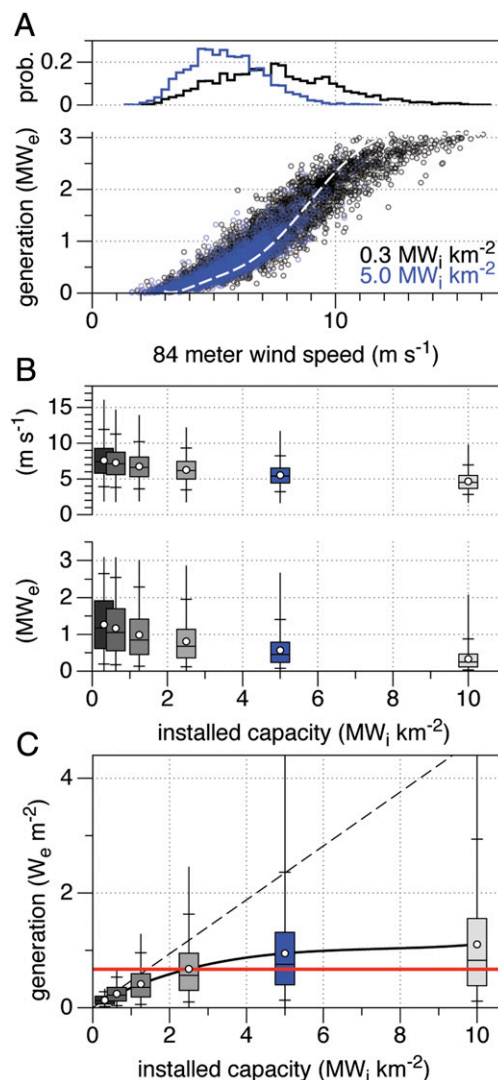


Fig. 2. (A) The per-turbine electricity generation rate for two select WRF simulations as a function of hub-height wind speed at 84 m as well as its histogram (Top). The dashed line shows the Vestas V112 3.0 MW_i power curve of a single turbine. (B) Mean per-turbine generation rate and the 84 m mean hub-height wind speed of the wind farm region as a function of installed capacity. (C) Mean per-turbine electricity generation rate as a function of installed capacity when the capacity factor of a single turbine is extrapolated to high installed capacities (dashed line, “no interactions”) and the relationship derived from the WRF simulations (solid line, “interactions”). The red line shows the VKE estimate. All box-whisker plots show the 5, 25, 50, 75, and 95% values, with the extent showing the minimum–maximum and the circles showing the mean.

highly correlated: $r^2 = 0.98$, with a slope of $m = 1.76$, an rmse of 0.60, and a mean absolute error (MAE) of 0.47. The WRF estimate from the $5.0 \text{ MW}_i \cdot \text{km}^{-2}$ simulation, an installed capacity often used for wind power planning and policy analysis (6), also compares very well, with daily mean estimates being highly correlated with VKE with $r^2 = 0.98$, $m = 1.47$, $\text{rmse} = 0.39$, and $\text{MAE} = 0.32$. The mean generation rate of this WRF simulation was $0.95 \text{ W}_e \cdot \text{m}^{-2}$, nearly the same rate as the $10 \text{ MW}_i \cdot \text{km}^{-2}$ simulation, but from half the number of turbines. When hourly estimates of WRF and VKE are compared (Fig. 3), we note that correlations are very high during day and night, but the slope is much better captured by VKE during the day, whereas at night VKE underestimates the magnitude of electricity generation by almost 45% in this simulation.

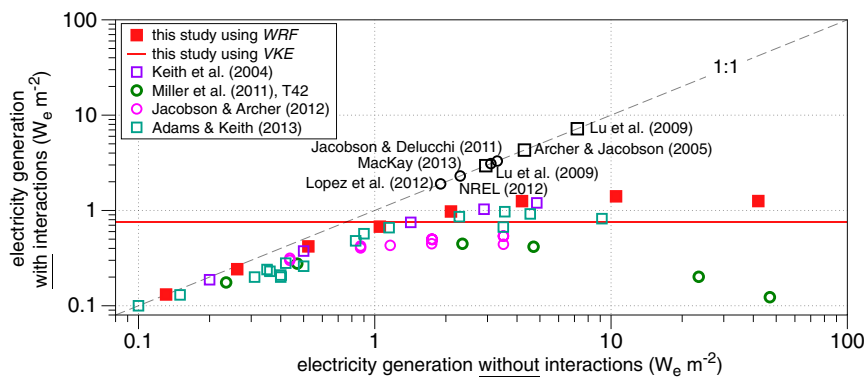


Fig. 5. Regional (squares) and continental-to global scale (circles) large-scale electricity generation estimates in relation to the effect of turbine–atmosphere interactions. The estimates represented by black squares and circles used preturbine wind speeds without including turbine–atmosphere interactions and are placed on the 1:1 line for reference. The colored points refer to estimates based on atmospheric models. These estimates simulate wind speeds and include turbine–atmosphere interactions (y axis). The value on the x axis was derived from using the turbine power curve, installed capacity, and the wind speeds of the control simulation. The horizontal line at $0.64 \text{ W}_e \text{ m}^{-2}$ with interactions is the VKE estimate for Kansas (based on figure 4 from ref. 12 with additional studies and the VKE estimate added).

$2.9 \text{ W}_e \text{ m}^{-2}$ ($0.8\text{--}6.6 \text{ W}_e \text{ m}^{-2}$) from a mean installed capacity of about $11 \text{ MW}_i \text{ km}^{-2}$ ($3.5\text{--}24 \text{ MW}_i \text{ km}^{-2}$). These generation rates are substantially higher than our $1.1 \text{ W}_e \text{ m}^{-2}$ limit of large-scale wind power generation in Kansas, although the size of the wind farms is also notably smaller.

This difference in wind power generation rates can be understood by relating the kinetic energy used by the wind turbines to their sources. For this, we distinguish between the import of kinetic energy by horizontal and vertical fluxes into the wind farm region. These two contributions change as the spatial scale of the wind farm increases. This change can be illustrated by using the mean values of the wind farm region from the WRF control simulation over the 4-mo period. The mean horizontal flux of kinetic energy is given by $KE_{in,h} = (1/2)\rho v_0^3 \cdot x \cdot h$, where $\rho = 1.1 \text{ kg m}^{-3}$ is the air density at hub height, $v_0 = 8.0 \text{ m s}^{-1}$ is the hub-height wind speed at 84 m, $x = 360,000 \text{ m}$ is the east–west extent of the wind farm that is perpendicular to the mean wind direction, and $h = 112 \text{ m}$ is the height of the wind farm, assumed here to be equivalent to the rotor diameter of the 3.0 MW_i turbine. This yields a mean horizontal kinetic energy flux of $KE_{in,h} = 11 \text{ GW}$ (or 282 W m^{-2} per unit cross-sectional area) into the upwind vertical cross-section of the wind farm region. The mean vertical kinetic energy flux is given by $KE_{in,v} = \rho u_*^2 \cdot v_0 \cdot x \cdot y$, where the mean (spatial and temporal) friction velocity at the surface $u_* = 0.45 \text{ m s}^{-1}$ and $y = 312,000 \text{ m}$ is the north–south extent of the wind farm that describes the downwind length of the wind farm. This yields a mean vertical kinetic energy flux downward into the entire wind farm region of $KE_{in,v} = 200 \text{ GW}$ or 1.8 W m^{-2} per unit surface area of the wind farm region, so that in the Kansas setup, $KE_{in,v}$ provides about 20 times as much kinetic energy as the horizontal influx. Note that this vertical flux of kinetic energy, derived from the WRF control simulation, served as the input to the VKE estimate. When the wind farm increases in downwind length with a greater value of y , the contribution by the vertical kinetic energy flux into the wind farm region increases linearly whereas the horizontal contribution remains relatively unchanged. WRF simulations with an installed capacity of $1 \text{ MW}_i \text{ km}^{-2}$ or greater ($>110 \text{ GW}_i$) represent wind farms in which the installed capacity is of the order of the mean kinetic energy flux into the wind farm region (about 211 GW), which is when the reductions of wind speed start to play a role in shaping the generation rate.

In the context of the Kansas wind farm region, we can use these considerations to estimate the downwind depth at which the horizontal kinetic energy flux is fully consumed by electricity generation and turbulence. Assuming a conservative 33% loss to turbulence during the extraction process (25), the 11-GW mean horizontal kinetic energy flux would result in a maximum electricity generation rate of 7.4 GW_e . This generation rate is equivalent to about 5,800 wind turbines of 3.0 MW_i capacity with a 42% capacity factor, which is close to our WRF simulation at the lowest installed capacity of $0.3 \text{ MW}_i \text{ km}^{-2}$. When considering the much greater installed capacity of $5.0 \text{ MW}_i \text{ km}^{-2}$, the 11 GW

of horizontal kinetic energy flux would be fully consumed within a downwind depth of about 10 km (see also ref. 22). Therefore, as the downwind extent of the wind farm grows, electricity generation rates of successive downwind turbines are derived progressively less from the horizontal flux and more from the vertical flux. This results in an edge effect of higher generation rates at the upwind border of the wind farm compared with lower generation rates in the interior of the wind farm region (see also *SI Appendix, Fig. 9*). This edge effect does not exist for the VKE estimate (*SI Appendix, Fig. 9*), because it neglects the horizontal kinetic energy flux as an energy source. This can in part explain the lower estimates of the VKE method. However, when considering wind farms of greater sizes, the influence of this edge effect on the mean generation rate becomes progressively less important to consider.

Generation rates above those estimated by VKE could be achieved if the incoming horizontal kinetic energy flux is available to the wind farm because it was not extracted by upwind turbines, or relate to an increase in the vertical kinetic energy flux by the wind turbines, as shown to particularly occur in the WRF simulations at night. The spatial extent over which this enhanced vertical kinetic energy flux can be maintained, how much it alters the LLJ, and possibly how this results in a regional redistribution in this flux remain as open questions.

An overall increase in the downward kinetic energy flux at larger deployment scales seems unlikely to occur, because climate model simulations performed at continental and global scales do not predict such an increase for present-day radiative forcing conditions (10, 13). Although these studies did not include a full analysis of the energetics, their predictions broadly agree with the predictions of the VKE method in terms of a maximum of 25–27% of the natural dissipation rate that could be used for electricity generation (10) and a slowdown of hub-height wind velocities by 51% globally, 50% over land, and 51% over the ocean (13). Despite its lack of considering changes in the downward kinetic energy flux, it would nevertheless seem that the VKE method is suitable to provide first-order estimates of the magnitude of wind power generation by large wind farms, but this would require further confirmation.

This agreement does not resolve the apparent discrepancy between our estimates and the observation-based estimates from small UK wind farms (38); note that these wind farms have downwind depths much less than 10 km , making their electricity generation rates almost exclusively dependent on the horizontal kinetic energy flux. Formulated differently, edge effects determine the generation rate of these small wind farms. To illustrate compatibility with WRF-simulated results, we apply the footprint area definition of ref. 38 for isolated 3.0 MW_i wind turbines (i.e., a circle with diameter five times the turbine diameter, or 0.25 km^2 per turbine) to our simulation of $0.3 \text{ MW}_i \text{ km}^{-2}$. This results in each 3.0 MW_i turbine being spaced 3.1 km apart and yields a comparable

5.1 $W_e \cdot m^{-2}$ for the turbines. For progressively larger installed capacities, this estimate decreases to 4.7 $W_e \cdot m^{-2}$ for an installed capacity of 0.6 $MW_i \cdot km^{-2}$, to 4.0 $W_e \cdot m^{-2}$ for 1.3 $MW_i \cdot km^{-2}$, to 3.3 $W_e \cdot m^{-2}$ for 2.5 $MW_i \cdot km^{-2}$, to 2.3 $W_e \cdot m^{-2}$ for 5.0 $MW_i \cdot km^{-2}$, and to 1.3 $W_e \cdot m^{-2}$ for 10 $MW_i \cdot km^{-2}$.

In summary, these considerations illustrate the strong dependence of small-scale wind farms on a horizontal kinetic energy flux that is not influenced by other wind farms upwind. Our results suggest that expanding wind farms to large scales will limit generation rates by the vertical kinetic energy flux, thereby constraining mean large-scale generation rates to about 1 $W_e \cdot m^{-2}$ even in windy regions. Large-scale estimates that exceed 1 $W_e \cdot m^{-2}$ thus seem to be inconsistent with the physical limits of kinetic energy generation and transport within the Earth's atmosphere.

Conclusion

We evaluated large-scale limits to wind power generation in a hypothetical scenario of a large wind farm in Kansas using two distinct methods. We first used the WRF regional atmospheric model in which the wind farm interacts with the atmospheric flow to derive the maximum wind power generation rate of about 1.1 $W_e \cdot m^{-2}$. This maximum rate results from a trade-off by which a greater installed capacity resulted in a greater reduction of wind speeds within the wind farm. This reduction in wind speeds reflects the strong interaction of the wind farm with the atmospheric flow, with speeds reduced by 42% at the maximum generation rate. We then showed that these estimates can also be derived by the VKE method, which used the downward influx of kinetic energy of the control climatology and its partitioning into turbulent dissipation and wind-energy generation as a basis. The

VKE method predicts that the maximum generation rate equals 26% of the instantaneous downward transport of kinetic energy through hub height. This method only required the information of wind speeds and friction velocity of the control climate to provide an estimate of a maximum wind power generation rate. With an estimate of 0.64 $W_e \cdot m^{-2}$, the VKE method underestimates the maximum wind power generation rate, particularly during night, but it nevertheless captures the temporal dynamics as well as the reduction in wind speeds very well.

Both methods used here yield estimates for the limits to large-scale wind power generation that are energetically consistent. Although many current wind farms are still comparatively small and can therefore sustain greater generation rates, an energetically consistent approach becomes relevant when the installed capacity of the wind farm approaches the kinetic energy flux into the wind farm region. Although the VKE method assumes this influx to be fixed, it nevertheless demonstrates that an energetically consistent estimate can be done in a comparatively simple way, thus providing a useful means to derive a first-order estimate of large-scale wind power generation from preturbine climatologies. We conclude that large-scale wind power generation is thus limited to a maximum of about 1 $W_e \cdot m^{-2}$ because of this inevitable reduction of wind speeds and the comparatively low vertical kinetic energy fluxes in the atmosphere.

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